

Modelling contact mode and frequency of interactions with social network members using the multiple discrete-continuous extreme value model

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ABSTRACT

Communication patterns are an integral component of activity patterns and the travel induced by these activities. The present study aims to understand the determinants of the communication patterns (by the modes face-to-face, phone, e-mail and SMS) between people and their social network members. The aim is for this to eventually provide further insights into travel behaviour for social and leisure purposes. A social network perspective brings value to the study and modelling of activity patterns since leisure activities are influenced not only by traditional trip measures such as time and cost but also motivated extensively by the people involved in the activity. By using a multiple discrete-continuous extreme value model (Bhat 2005), we can investigate the means of communication chosen to interact with a given social network member (multiple discrete choices) and the frequency of interaction by each mode (treated as continuous) at the same time. The model also allows us to investigate satiation effects for different modes of communication. Our findings show that in spite of people having increasingly geographically widespread networks and more diverse communication technologies, a strong underlying preference for face-to-face contact remains. In contrast with some of the existing work, we show that travel-related variables at the *ego* level are less important than specific social determinants which can be considered while making use of social network data.

Keywords: social network analysis; multiple discrete continuous; snowball sample

1. INTRODUCTION

In the activity-travel perspective, travel is a derived demand due to activities (Ortúzar and Willumsen, 2011). Individuals connect the activities in their lives by travel because they bring value to their life. This is because activities “satisfy a particular need or requirement” (Ortúzar and Willumsen, 2011, p. 473). The need to socialise is a basic human need and travel serves to bring individuals together through face-to-face interaction. Carrasco and Miller (2006, 2009) developed conceptual models of social activity generation and social

network structure and information and communication technology (ICT) interaction. Habib and Carrasco (2011) declare that their work suggests that “activity scheduling models should explicitly include the role of social networks” (p. 2). Lin and Wang (2014) found that emotional support from family led to more joint travel trips as compared to emotional support from non-family friends and acquaintances. Castiglione et al. (2015) note that activity-based models at the academic level have considered full social networks in joint travel decisions and in generating and scheduling daily tours, but their use in practice-ready activity-based models has not been implemented yet.

This need for socialising can also be achieved by other forms of communication. Often, these communication patterns are correlated by different modes of communication and travel (van den Berg et al., 2012a; Frei and Axhausen, 2009; Kowald, 2013; Lin and Wang, 2014; Schaap et al., 2016; Tillema, 2010). Thus, communication patterns are an integral component of activity patterns and the travel induced by these activities. Understanding the determinants of communication patterns between people and their social network members is critical for gaining further insights into travel behaviour for social purposes. A social network perspective brings value to the study and modelling of activity patterns since social activities are influenced not only by traditional trip measures such as time and cost but also motivated extensively by the people involved in the activity (Ryley and Zanni, 2013). Van den Berg et al. (2012b) provide an extensive review connecting social networks, ICT use for social interaction and communication patterns:

- The majority of social network studies in transportation use egocentric social network data. These approaches prompt users with a name generator to create a list of relevant contacts. By following this up with questions about the given contacts, measures of an individual’s social network can be formed including network-wide measures (e.g. centrality, density, between-ness) as well as dyad-level measures (characteristics of the linkage between two individuals).
- There is still limited research on the impacts of ICT use on social activity generation. Support for the substitution hypothesis of ICT use replacing all face-to-face communication is limited. In contrast, studies have found a complementarity between ICT use and social activity generation.
- Communication mode and frequency have been found to be impacted by not only individual characteristics, but also by dyad-level attributes such as tie type and relationship, tie strength and geographic distance.

For example, previous research has found relationships between face-to-face social activity and online social activities (Schaap et al., 2016). In research by Schaap et al. (2016), increasing internet usage was correlated with increasing network sizes, distances between friends, and increasing travel distances for social activities. But they also found that increasing online social activities reduced some specific types of social travel (e.g. out-of-home entertainment). The authors conclude that these effects are not simple or one-

directional and that “the complexity of the activity and the context-dependency lead to a complex set of simultaneous effects” (p. 12).

Previous research mainly used multi-level models (Frei & Ohnmacht, 2014) to address the complexities in communication mode choice and frequency. This hierarchical structure accommodates different “levels” with different dependent variables, namely the frequency of interaction, the *ego*-level characteristics and the *ego-alter* dyad ones. Van den Berg et al. (2012a) used multilevel path analysis to describe mode-specific communication frequencies and correlations between modes. Their results indicated a complementary relationship between the communication frequencies between the modes. The authors state that “the contact frequencies of the different modes, especially face-to-face and telephone, can also be largely explained by the *ego*’s personal characteristics and the type of relationship and the distance between *ego* and *alter*” (p.125). Frei and Axhausen (2009) perform a similar multilevel path analysis to describe communication mode and frequency relationships. Frei (2012) notes a limitation of path analysis techniques in that the models are fitted on sample covariance rather than sample values.

In contrast, a multivariate regression approach can be used to fit a model on sample values. Frei (2012) and Kowald (2013) used multivariate multilevel linear regression models of dyad-level communication patterns. Frei’s (2012) results showed that:

- Increases in distance correspond to decreases in face-to-face and phone contact frequency while e-mail frequency is unaffected.
- *Ego*-level socio-demographics were more influential than dyad-level (*ego-alter*) characteristics.
- “The interaction of the different contact modes and face-to-face meetings are complementary” (p. 137).

Kowald (2013) also reports similar results and additionally found that nuclear family members and close social ties were contacted more frequently than other contacts. But the multivariate linear regressions used in that work have limitations due to the skewness in mode frequency data. This is due to high incidences of no communication via a mode and because some contact frequencies occur at very high levels. In these studies, the authors dealt with this concern by either removing observations (mode-level) for an *ego-alter* communication mode if no communication was performed via that mode (Kowald 2013), or using a log-transformation with a residual maximum likelihood estimator and setting communication frequencies of zero to the minimum positive frequency for that mode (Frei 2013). Either of these approaches is unsatisfactory and this is a further motivation for the approach used in our work.

Neither the path analysis approach nor the multivariate regression approach account for behavioural conditions that lead to zero communication frequency. Overall, these prior models are unable to describe why individuals would choose to not communicate by a

certain mode, but only describe how much communication occurred if the mode was chosen.

The present study aims to account for this limitation by explicitly modelling the selection of communication mode and its corresponding communication frequency. In our work, we simultaneously take into account potential determinants of the decision at both the *ego* and the *ego-alter* level. By using a multiple discrete-continuous extreme value model (Bhat 2005), we can simultaneously investigate the mode of communication chosen to interact with a given network member and the frequency of interaction by each mode. The model further allows us to investigate satiation effects from different modes of communication. The multiple discrete component of the model accommodates the fact that each ego potentially communicates with multiple alters and using different modes of communication. The continuous component of the model accommodates the fact that for each alter and mode and communication, there is the possibility of either 0, one, or multiple interactions. Of course, the number of times an ego communicates with an alter using a given mode is an integer value in the data, and the use of a continuous response model thus represents somewhat of an abstraction from reality. This is however no different in regression work.

The paper is organised as follows. The next section introduces the dataset used for the study. Section 3 provides an overview of the modelling framework, with an emphasis on the role of the different utility function parameters, before presenting the specification used in our analysis. The fourth section presents the results of the model estimation and provides an interpretation of the specific coefficients and their impact on behaviour, while the fifth section shows a simple forecast example on the basis of the estimated model. The final section draws conclusions and implications for travel behaviour analysis and outlines the next steps to be taken in the study of this topic.

2. Data

2.1. Survey overview

Over the past decade, the field of transport planning has been using methods from social network analysis to approach and explain leisure travel (see Larsen et al., 2006; Carrasco 2006; Frei and Axhausen 2007; van den Berg et al., 2009, Kowald & Axhausen 2014).

The selection of this methodological approach is based on the recognition of leisure travel as being primarily undertaken to join others in leisure activities. For this reason, leisure travel is also referred to as 'social' or 'activity' travel. Existing work analysed correlations between characteristics of network topology (for example the number of social contacts and geographical distances between people) and aspects of travel activity, resulting in new empirical findings (Larsen et al., 2006, Carrasco et al., 2008, Silvis et al., 2006, Frei and Axhausen, 2007 and Kowald & Axhausen 2014) as well as suggesting advances to overcome the challenges in data collection and modelling (Frei and Axhausen, 2008, Hogan et al., 2007 and Carrasco et al., 2008). These studies though did not try to survey a population-wide 'global' leisure network, but only looked at individual 'ego-centric' networks. Knowledge of

the wider network structure connecting personal networks to form a population-wide one allow more generalizable analyses as well as the implementation of a ‘global’ leisure network in agent-based travel demand simulations.

The Institute for Transport Planning and Systems (IVT) of ETH Zurich conducted a survey between January 2009 and March 2011 to investigate this global leisure network topology, as part of a joint project with the Institute for Sea- and Land-Transport (ILS) of TU Berlin.

One way of obtaining a population-wide leisure network is to sample respondents by means of a ‘chain method’, in which some initial respondents are asked to report their social contacts and these contacts are in turn used to enlarge the network sampled. The survey implemented to collect the data used in this paper makes use of one of the best-known chain methods, ‘snowball sampling’, which implies asking initial respondents, called “seeds”, to report their social contacts. These social contacts are then again asked to report their social contacts and invite them to take part in the study, a procedure that can be repeated for a predefined number of iterations. With the exception of the seeds, all respondents in a snowball sample are reported by former respondents. An illustration of a network obtained by a snowball chain is given in Figure 1.

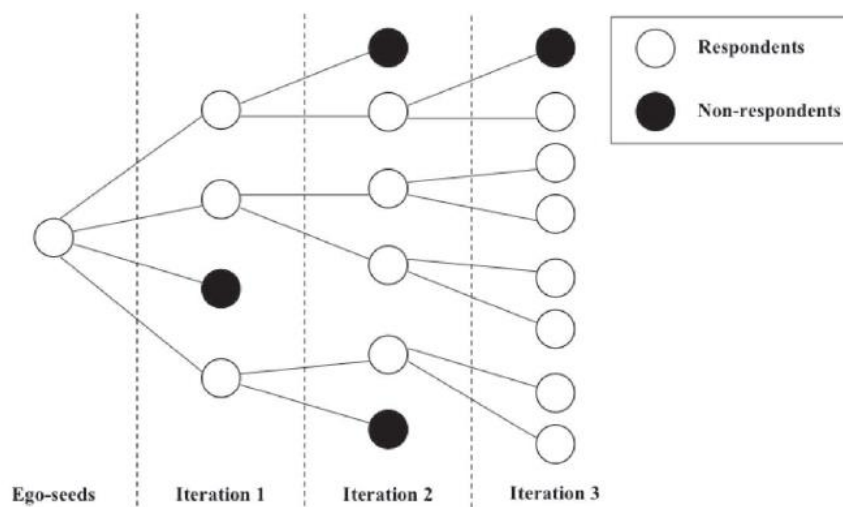


Figure 1: An illustration of a three-iteration snowball chain.

Source: Kowald & Axhausen (2012)

Snowball chains were started with 40 *ego*-seeds drawn from a stratified random sample of the Canton Zurich population. Half of the seeds got to the second iteration of *egos* (who named *alters* constituting the third iteration). The remaining 20 chains included iteration 3 *egos*, and the researchers who collected the data were planning to let the snowball chain continue until iteration 4. Respondents can report social contacts anywhere, so that recruitment is not geographically limited.

The survey instrument was made up of four sections.

- The first section included questions about respondents' socio-demographics and mobility biography, i.e. a report of the places where they lived and worked throughout their lives.
- The second section was made up of two name generators. Name generators are questions, generally in the form of tables, which ask people to report names of their social contacts. The wording of the question makes use of specific stimulus to help respondents focus on the part of their social network of interest to a study and recall all the relevant names (Marsden, 1990, Campbell and Lee, 1991 and Wolf, 2004).
The use of two name generators is motivated by the need to use different stimulus for a complete and more accurate recall of the social network of interest. The first name generator asks explicitly for leisure contacts providing examples related to leisure interactions, which should guide respondents in distinguishing whether a relationship fits to the requirements or not. The second name generator applies a different approach, as it asks respondents to mention the people with whom they discuss important problems. The question asked in relation to the second name generator differs from the one used in the first one in that it uses an affective perspective instead of a stimulus about the context of social interactions. Although the latter might be subject to individual interpretation, contacts from both name generators can trigger leisure travel and are therefore relevant given the scope of the study. The social network reported through the two name generators could not exceed the size of 40 contacts, but participants were encouraged to use additional sheets of paper if needed. In most analyses of the present dataset (Illenberger et al. 2011, Kowald & Axhausen 2012), including the one in the present paper, we only make use of the first 40 contacts to avoid potential bias deriving from the extra effort some participants made to report names in a non-survey form.
- The third instrument used in the survey was a 'name interpreter', where *egos* were asked to enrich the list of names reported in the name generators by adding *alters'* socio-demographics as well as information related to the *ego–alter* relationship, e.g. duration and circumstances of first meeting.
To ensure continuation of the snowball recruitment, named social contacts' addresses were collected so that the survey and an optional invitation card could be sent to them. Only a paper version of the survey was in fact administered, therefore physical addresses were necessary to communicate with participants.
- The fourth section of the survey was a 'sociogram', a tool used to indicate whether, among the social contacts mentioned in the name generators, there were groups of people who know each other and generally spend time together. The information collected through this last section is not used for the current work.

As this type of survey could appear quite unusual to respondents, special care was taken of question formulation, so that potential sources of misinterpretations were avoided. Where a risk of misunderstandings was identified, examples were provided to clarify the question. Another potential problem with this type of survey is that respondents might not be comfortable with providing information (especially home addresses) about their social contacts. Several measures to establish trust between respondents and the survey promoters were adopted. *Egos* were asked to sign an invitation card to be sent to their *alters* by the research team (for more details see Kowald et al., 2009), and once they had agreed to take part, the survey instrument was sent to them together with a 20 CHF (approximately €19 in 2015) monetary incentive. A response rate of 26% was achieved and considered satisfying by the promoters. Although some fatigue effects are present in the responses, the share of missing values is low, around 3% for *egos*' and 13% for *alters*' characteristics (for details see Kowald et al., 2010). As mentioned above, the sample had no predetermined geographical limits, but despite this setting most respondents were from the German speaking part of Switzerland. Although data cleaning and censoring somewhat limited its representativeness, the originally collected sample matched the characteristics of the Swiss population well.

For further information and details about the data collection protocol, see Kowald & Axhausen (2014).

2.2 Sample characteristics

We excluded from the analysis all the *egos* who did not report any frequency of communication with any of their network members. We also excluded *egos* for whom most of the basic socio-demographic information were missing. Our final sample is made up of 638 *egos*, who named 13,500 *alters*. The socio-demographic and economic characteristics of the *egos* are reported in Table 1.

Number of <i>egos</i> = 638 Number of dyads= 13,500		
	N	%
<i>Sex</i>		
Male	245	38%
Female	389	61%
<i>Age</i>		
Age = 18	4	1%
Age 19-30	47	7%
Age 31-45	149	23%
Age 46-60	258	40%
Age > 60	149	23%
<i>Car availability</i>		
Always	60	9%
Often	90	14%
Seldom	46	7%

Never	21	3%
<i>Civil status</i>		
Married	461	72%
Divorced	51	8%
Living separately	8	1%
Single	90	14%
Widowed	27	4%
<i>Employment status</i>		
Student	19	3%
Employed full time (FT)	210	33%
Employed part time (PT)	231	36%
Homemaker	70	11%
Retired	96	15%
Looking for work	10	2%
Unfit to work	1	0%
<i>Citizenship</i>		
Switzerland	576	90%
Germany	18	3%
Italy	11	2%
Austria	5	1%
France	4	1%
Other	21	3%
<i>Household income (CHF)</i>		
Min	0	
Max	18000	
Average	10320	
<i>Education duration (years)</i>		
Min	0	
Max	35	
Average	14.94	
<i>Network size (number of contacts)</i>		
Min	1	
Max	40	
Average	21.16	

Table 1 – Descriptive statistics of the sample

Note that we consider as an *ego* any respondent who has completed the entire survey and named her (or his) *alters*, no matter the wave in which she was recruited. In this sense, we virtually make use of *egocentric* data despite the fact that the dataset has been collected as a snowball sample.

The independent variables included in the modelling work are characteristics of both *ego* and dyad, i.e. features of the relationship between the *ego* and each *alter*. The list of *ego-alter* measures used in the model (excluding missing values) is given in Tables 2 and 3. Table

2 reports continuous measures and their basic statistics, while Table 3 reports categorical variables. Note that the statistics for distance between *ego* and *alter* includes only “positive” distances, i.e. people who live together are excluded. As stated above, missing values are excluded from these tables (this is why the percentages do not sum to 100%) although a specific treatment has been adopted in the modelling, as detailed in section 4.2.

	Mean	Median
<i>Distance (km)</i>		
	2,817.57	8.68
<i>Age difference (years)</i>		
	16.51	15
<i>Relationship duration (years)</i>		
	21.27	19

Table 2 – continuous dyad measures

	N	%
<i>Sex homophily</i>		
Both male	2,981	22%
Both female	5,810	43%
Different sex	4,269	32%
<i>Help & Discuss</i>		
Ask for help	4,474	33%
Discuss problems	7,120	53%
<i>Type of relationship</i>		
Spouse	308	2%
Relative 1st degree	1,845	14%
Other relative	819	6%
Married into family	705	5%
Friend	5,685	42%
Acquaintance	3,717	28%
<i>Citizenship homophily</i>		
Same citizenship	10,935	81%
Different citizenship	1,263	9%
<i>Education homophily</i>		
Same level	6,729	50%
Different level	4,430	33%

Table 3 - categorical dyad measures

3. Methodology

3.1. MDCEV framework

The family of MDCEV models first proposed by Bhat (2005) and extended in different directions (Bhat 2008, Pinjari and Bhat 2010, Castro et al. 2012) represents the state of the art in modelling multiple discrete-continuous choices. The initial exponential utility function proposed in Bhat (2005) was later replaced in most application by a Box-Cox specification which presents several advantages, as described in Bhat (2008); in particular, the continuity of the Box-Cox form with respect to the exponent, even for values near zero, turned out to be important in our work.

The Multiple Discrete Continuous Extreme Value (MDCEV) model and its various extensions have been applied to several empirical contexts, mainly related to the study of travel behaviour. Examples are applications to the choice of vehicle type and mileage (Bhat and Sen, 2006; Sen 2006), to the type or timing and duration of activities (Bhat 2005, Srinivasan and Bhat 2005, Pendyala and Bhat 2004) and to vacation-related decisions (Pinjari and Sivaraman 2013). The model has also been used in applications other than transport. For example, Lu et al. (2015) have applied it to the case of multi-buy alcohol promotions. Woo et al. (2014) used the model to understand how the use of traditional media (e.g. television, radio, newspaper) had been affected by new ones, such as in-home and mobile internet. Another application to media use is Block and Schultz (2015), focussed on understanding the time spent on each medium (television, radio, print, internet) by American consumers. The present paper represents the first application of the present modelling framework to investigate patterns of social interaction between people and their social contacts.

The model is derived coherently with the random utility maximisation theory, and it differs from traditional choice models in the fact that, by allowing the choice of multiple products, it relaxes the assumption of the alternatives being mutually exclusive. The additive but non-linear formulation of the utility function guarantees that the consumption of one good does not affect the utility of the others and that these goods are imperfect substitutes. The non-linear specification allows estimation of the satiation experienced from each good by allowing for diminishing marginal returns. The derivation of probabilities also differs from standard choice models.

The presence of both a discrete and a continuous choice dimension allows the modelling of the behaviour of people choosing a number of different options at the same time (for example varieties of products sold on the market) and, for each of them, a continuous amount to consume, for example money or time spent making use of them. They make their consumption decisions in order to maximise a direct utility function $U(\mathbf{x})$, where \mathbf{x} is a vector of non-negative quantities of consumption for each of the goods, $\mathbf{x} = (x_1, \dots, x_K)$. The expenditure that an individual can allocate to the purchase of the goods is subject to a budget constraint $\mathbf{x}\mathbf{p} = E$, where E is the budget, and \mathbf{p} is the vector of prices. In most applied work, as well as in our case, \mathbf{x} includes a unit-priced outside good to represent expenditure on a good that is always consumed in a positive quantity by all the individuals in the sample. This can have a specific interpretation or simply represent the consumption of all the other goods on the market.

The functional form of the direct utility is a generalised variant of the translated CES function, additive with respect to the different products but non-linear to allow diminishing marginal returns, i.e. that the benefit of an additional unit purchased of a given good decreases with increasing consumption of that good. The utility formulation, introduced by Bhat (2008), assumes the presence of K goods and assumes good 1 to be the outside good, although this choice is fully arbitrary. The utility function is as follows.

$$U(x) = \frac{1}{\alpha_1} \psi_1 x_1^{\alpha_1} + \sum_{k=2}^K \frac{\gamma_k}{\alpha_k} \psi_k \left(\left(\frac{x_k}{\gamma_k} + 1 \right)^{\alpha_k} - 1 \right)$$

so that $U(\mathbf{x})$ is a quasi-concave, increasing and continuously differentiable with respect to \mathbf{x} and ψ_k , γ_k , and α_k are parameters relating to good k .

The specific role of these parameters is as follows.

- ψ_k is defined as the 'baseline utility of good k '. It is in fact the marginal utility of the good at the point of zero consumption. A higher baseline utility makes corner solutions (i.e. zero consumption of a good) less likely. ψ_k is a function of observed characteristics z_k associated with good k and the decision maker. z_k also includes a constant reflecting the generic preference for good k . The random form of the utility is obtained by introducing an exponential multiplicative random element. This, together with an exponential form of the deterministic component of utility, ensures the positivity of the utility, which can be written as: $\psi(z_k, \varepsilon_k) = e^{\beta' z_k + \varepsilon_k}$, where ε_k is an extreme value error term, and β is an estimated vector of parameters. For identification, we set the deterministic part of the log baseline utility for one good to zero, say the outside good.
- The γ parameters in the model have several roles. First, they are translation parameters that allow for corner solutions, so that for any good (other than the outside good) it is possible to evaluate the model with $x = 0$. Second, γ defines a scale for each good. Third, because γ defines a scale, it also affects the satiation, as a higher γ_k implies that more consumption of the corresponding x_k is needed to obtain the saturation effect. It is this last role of γ that makes separate identification of γ and α difficult.
- α_k is a 'pure' satiation parameter. By exponentiating the consumption quantity of good k , it reduces the utility of any additional unit consumed. α_k can take any value smaller or equal to 1. Low α_k means faster satiation. In our model, we bound $0 \leq \alpha_k \leq 1$ as suggested by Bhat (2008). When $\alpha_k \rightarrow 0$, the utility form above collapses to a linear expenditure system (see Bhat, 2008). Conversely, $\alpha_k = 1$ would reproduce the case of 'traditional' choice models, i.e. with constant marginal utility of consumption and no satiation effects allowed.

As mentioned above, both α_k and γ_k control satiation although through different mechanisms, as the former does so by exponentiating the consumption quantity while the latter by translating it. Bhat (2008) argues that the two effects are very hard to disentangle in empirical analysis, and for this reason some form of normalisation is generally needed. Indeed, he claims only three different versions of the stochastic model, obtained by fixing some of the parameters, are empirically estimable. In the present application, we have

made use of the γ -profile (cf. Bhat 2008), which estimates the α parameter for the outside good only with other α parameters taking the zero limit and all $\gamma_k, k > 1$.

The probability that an individual consumes the quantities $x_1^*, x_2^*, \dots, x_M^*, 0, \dots, 0$, where M of the K goods are consumed in positive amounts, is given by (see Bhat, 2008):

$$P(x_1^*, x_2^*, \dots, x_M^*, 0, \dots, 0) = \frac{1}{p_1} \frac{1}{\sigma^{M-1}} \left(\prod_{m=1}^M f_m \right) \left(\sum_{m=1}^M \frac{p_m}{f_m} \right) \left(\frac{\prod_{m=1}^M e^{V_i/\sigma}}{\left(\sum_{k=1}^K e^{V_k/\sigma} \right)^M} \right) (M-1)!$$

where σ is an estimated scale parameter and where $f_m = \left(\frac{1-\alpha_m}{x_m^* + \gamma_m} \right)$.

3.2. Application to social network data

The MDCEV model can accommodate the fact that people choose simultaneously between different products, in our case the means of communication with every member of their social network (face-to-face, phone, e-mail, SMS) and the quantity of each, in our case the frequency of interaction. We believe that this framework is more adequate than previous approaches to represent real-world behaviour in this specific case. The choice of how and how frequently to stay in touch with someone requires joint consideration of the *ego* and *alter* characteristics, and the understanding of underlying behaviour would be limited without considering the substitution effects that are likely to be present in this context.

The dependent variable of our model is the frequency of interaction by each communication mode with each social network member per year. As there are 4 possible modes of communication (face-to-face, phone, e-mail, SMS) and each *ego* can have at most 40 social contacts, the number of “products” in our model is $4 \times 40 = 160$. As not all the *egos* have named 40 social contacts, in the case in which someone has reported a lower number, say n , the remaining $40-n$ contacts are considered to be unavailable to her. The outside good, that in the present context represents all the activities other than communication, takes the total number of products to 161.

As described above, the model framework assumes the presence of a budget constraint. Typically, this has been treated either as a time budget (Bernardo et al. 2015, Bhat 2005, Salem & Habib 2015, Sener and Bhat 2012), a money budget (Ferdous et al. 2010, Lu et al. 2015, Rajagopalan & Srinivasan 2008, Yu et al. 2011, Yu & Zhang 2015) or even separate time and money budgets (Castro et al. 2012, Pinjari & Sivaraman, 2013). Authors are increasingly recognising the difficulty with the definition of money budgets, where a simple hard constraint such as 24 hours a day for a time budget does not apply. Indeed, individuals may for example have different mental accounts for different products. The situation is further complicated in the case of work using stated preference data (such as in Lu et al., 2015) where arguments can be made that the expenditure observed for a given respondent may well be below their budget constraint (if the scenarios presented were not varied enough) or may be above the real world budget constraint (by being based on hypothetical choices). Recent work by Augustin et al. (2015) has put forward the idea of using regression

approaches to estimate a latent budget for vehicle miles travelled, while Dumont et al. (2013) proposed a latent budget approach for money budgets.

For our specific case study, we use a slightly different approach. Firstly, as neither costs nor durations for the different types of interactions are available, the definition of time or money budgets would be difficult. Secondly, the use of such an approach would be geared at aiming to model (and then predict) the overall level of interaction an ego undertakes. In our work, we focus instead on understanding how, with the overall annual number of communications being determined exogenously, an ego distributes these across alters and across modes of communication.

In the specification of the model, we need to specify costs for each ‘product’, and an overall budget. In our final specification, given the above, we use a unit cost for each ‘product’, i.e. the same cost applies to one phone call as to one face-to-face meeting, for example. The *budget* for a given ego is then simply given by the total annual number of communications that we observe for that ego in the data, across all alters and all modes. We maintain an outside good in our model specification and simply assign one unit of the budget for the outside good¹.

We are aware of the simplification implied by assuming a joint budget for all four communication modes, with the same unit cost for each mode. In reality, the cost (time and money) of face-to-face interactions, especially when two people live far away from each other, is likely to be much higher than the cost of sending that person an e-mail. To test the impact of these simplifying assumptions, we also estimated models with a number of different specifications for costs and the budget. We first tested the impact of the unit cost assumptions, by making face-to-face the most expensive mode, ahead of phone, sms and e-mail. We still allocated one unit to the outside good. Secondly, we tested the impact of the budget assumption and specifically the allocation to the outside good, where we estimated a model in which a generic fixed amount is allocated to the budget for each individual. The full details of these tests are reported in our online appendix². Neither of these departures had a significant impact on our overall findings, and we thus maintained the unit cost assumption, and a budget given by total expenditure across inside goods plus one unit for the outside good.

The final specification of the model has been obtained by first testing the performance of the different specifications that can be empirically estimated (according to Bhat 2008). As mentioned above, we adopt the “ γ -profile” of the model in estimation, i.e. we only estimate the γ_k for $k = 1, 2, \dots, n$ and α_1 for the outside good. This profile provides better statistical fit than either the “ α -profile” or the “ $\alpha - \gamma$ -profile” in this specific empirical application. As α_1 presented an extremely small and insignificant value in all the model specifications we

¹ This is for econometric reasons alone, as it is helpful to have one good that is always chosen.

² http://www.stephanehess.me.uk/papers/Calastri_et_al_2017_online_appendix.pdf

estimated, we decided to fix it to zero in order to avoid computational problems. As an example, in the latest model specification where it was estimated, its value was 0.001 with a t-statistic of 0.878. In very simple specifications, for example where only the structural parameters of the models, the constants and the distance coefficients were estimated, α_1 was equal to 0.000005 with a t-statistic of 0.057. As explained in Bhat (2008), $\alpha_k \rightarrow 0$, implies that the utility form collapses to a linear expenditure system, i.e. to a log utility formulation.

Moreover, as it would have been impossible to estimate a γ_k for each of the 160 inside goods, we only estimated four of them, one for each mode of communication, which were then reused across alters. In estimation, to ensure positive values, we work with $\gamma_k = e^{\log(\gamma_k)}$, with $\log(\gamma_k)$ being estimated. For the presentation of the results, we then apply the transform, and report γ_k .

4. Empirical results

We started off by estimating a base version of the model and systematically adding and combining variables on the basis of statistical significance, intuition and guidelines from previous studies.

Our results are displayed in Table 4, where the estimates and t-statistics of coefficients are presented. A detailed presentation and interpretation of results follows.

4.1. Core results

Baseline constants & γ parameters

The δ_k parameters represent the baseline preference constant component of the utility of each alternative, where they enter through an exponential into ψ_k . A higher value for δ_k thus leads to an increase in the baseline utility of alternative k . The γ_k parameters in turn determine, jointly with the baseline utilities ψ_k , the impact that each additional unit of consumption has on the contribution that the consumption of good k makes to the overall utility. All else being equal, including the socio-demographic effects being the same across products, we could state that increases in δ_k will lead to bigger increases in utility for each additional unit being consumed, while for γ_k , the opposite applies. What we then see from our results is that, if the socio-demographic impacts on baseline utilities are the same across modes (a point we will return to below), a face-to-face contact has more impact on the utility function than a contact by phone ($\delta_{face-to-face} > \delta_{phone}$ and $\gamma_{face-to-face} < \gamma_{phone}$). The impacts of an interaction either face-to-face or by phone is also stronger than that of e-mail or SMS. However, for the latter two, the ordering is less clear cut, as $\delta_{e-mail} < \delta_{sms}$ and $\gamma_{e-mail} < \gamma_{sms}$. With $\alpha_k \rightarrow 0$ in our models, the utility component $\frac{\gamma_k}{\alpha_k} \psi_k \left(\left(\frac{x_k}{\gamma_k} + 1 \right)^{\alpha_k} - 1 \right)$ reduces to a log specification, with $\gamma_k \psi_k \log \left(\frac{x_k}{\gamma_k} + 1 \right)$. Ignoring the socio-demographic effects and setting $\psi_k = e^{\delta_k}$, we can then see that the impact of a SMS

is always stronger than the impact of an e-mail. With bigger consumption, this difference increases. This is a direct result of the fact that satiation is stronger with lower γ_k . We then also note that satiation approaches more rapidly for a given number of contacts when they are by phone and especially face-to-face. Intuitively this appears reasonable, as people exhaust all the activities/communication they want to undertake with an alter in fewer face-to-face meetings than with other forms of communication, followed by phone. The γ parameters could also be thought of, to some extent, as representing the amount of time and the cost of setting up the communication by each mode.

Effect of ego-level characteristics

The *ego* level characteristics are in general not strongly significant, possibly indicating that measures of the attributes of just one of the two people involved in the interactions are not sufficient in explaining the communication frequency. Nevertheless, we will try to interpret the significant coefficients for each of the variables. For each *ego*-level variable, we estimated for coefficients, one for each communication mode. This approach allows us to observe the impact of that variable on mode-specific frequency of communication.

Age

A categorical variable represents the age of *egos*, as shown in Table 1. The category including people more than 60 years old is used as a base. The significant coefficients give some interesting insights: the e-mail coefficient for the youngest category is negative and significant, meaning that teenagers are less likely to use e-mail than people who are over 60. This result may seem counter-intuitive if we think about the familiarity of younger generations with ITC, but existing studies (e.g. Agosto et al., 2012) found that teenagers make a reduced use of e-mails and see it only as a mode to communicate with adults or in particularly formal communication.

People in their twenties resulted being less likely to communicate by phone (although the significance level is only 90%) and rather surprisingly also by e-mail than people more than 60 years old, while they are significantly more likely to send SMS with respect to the oldest group. The last point is also true for the 31-45 and the 46-60 years old categories, confirming that this mode is probably not used much by those over 60.

Education duration

A log transformation is applied to the years spent in education. As concluded by previous studies (Frei and Ohnmacht, 2014), this variable is not particularly relevant in explaining the frequency of social interaction. The only significant coefficient shows that the longer the time spent in education, the more likely someone is to communicate via e-mail. This could be motivated by the fact that people with a higher level of education often hold “office jobs” or have in general higher IT literacy due to their engagement in further education, and therefore are more likely to use their computer as a way to communicate.

Relationship status

The different categories considered for the *ego's* relationship status are 'single', 'married', 'widowed', 'divorced' and 'married but living separately'. 'Single' is used as a base, so all the coefficients should be interpreted as effects relative to this category. In line with results of studies on the impact of marriage on social life and contact with the family of origin (e.g. Sarkisian & Gerstel, 2008), we find that married people are significantly less likely to communicate by e-mail and SMS than single people. Although the literature also suggests an effect on physical interactions, we do not find the impact on face-to-face meetings as significant. Both widowed and divorced people get a lower benefit from communicating via SMS than singles. We also find a negative effect on communication via e-mail for widows. Although several explanations for this could be possible, one interpretation could be that widowed people are believed to intensify phone and face-to-face contacts to overcome their loss and reduce their use of impersonal communication for social purposes, especially in late stages of life (Utz et al., 2002).

Employment status

This variable specifies whether the *ego* is a student, looking for a job, a homemaker, a retiree or is employed (full or part time). The last 'employed' category is our base. Most of the coefficients are not significant, but we observe that retired people are significantly less likely to use e-mail and SMS than those in employment. This result does not contradict the findings reported in the "Age" section above, as the effect of the latter and that of employment status are separately controlled for, and the two categories of "retired" and "over 60" are not necessarily coinciding. The higher propensity to communicate of those who are in employment with respect to those who are not has been found in previous research (Frei and Ohnmacht, 2014).

Number of social network contacts

In line with previous findings (Frei and Ohnmacht, 2014; Dunbar, 2003) all the mode-specific coefficients show that the higher the number of social contacts in the network, the less the utility that accrues by communicating by any mode. The intuitive explanation is that social contacts require maintenance, so the bigger the network, the lower the number of interactions that people can have with each of their network members.

Ego characteristics excluded from the model

Several *ego*-level variables that previous studies have found to be relevant for social interactions have proved to be non-significant in our model. As an example, differently from Carrasco and Miller (2009), we did not include network measures in our final specifications, as even the most commonly used ones, such as *degree centrality*, *betweenness* and *density*, did not have a significant effect on communication frequency. We believe that this is due to the fact that the actual pattern of communication is mainly determined by characteristics of the two individuals involved in it, not necessarily by the overall network structure.

Different transformations were applied to the income variable to investigate potential effects but we never found it to be a significant determinant. We do not find this result too

unexpected. We appreciate that face-to-face contact with people who live far away could be rather costly, but lacking information on the spatial arena of each interaction, it would have been difficult to expect a specific effect.

We also excluded the variable indicating the availability of a car to the ego as we found no significant effects on patterns of communication. This variable had four levels (i.e., a car could always, often, seldom or never be available), and we attempted various specifications with these levels but no effect was found. We also tested possible interactions of this variable with others, namely civil status, employment status, level of education, presence of children in the household and number of social contacts, but no significant effect was found. This finding may be surprising, but a review of the existing literature reveals the lack of robust evidence about this effect. Frei & Axhausen (2009) and Frei & Ohnmacht (2014) find relatively weak positive effects of car availability on face-to-face interaction, while Tillema et al. (2010) and Sharmeen et al. (2014) find an effect of the number of cars on frequency of interaction. Other studies reached conclusions in line with ours, i.e. they do not find significant effects (Carrasco, 2011; van den Berg & Timmermans, 2015) or highlighted that car availability can have an effect on decisions other than frequency in the domain of social interactions, such as the decision of whether to interact (van den Berg et al., 2015) and the number of trips for social purposes (van den Berg et al., 2013). Moreover, van den Berg et al. (2012b) find that car ownership has no effect on frequency of interaction and only has a weak impact on the choice to communicate by phone. One possible interpretation of our findings could be related to the fact that the public transportation system in Switzerland is very efficient and relatively inexpensive. Somewhat surprisingly, the ownership of a public transport pass also did not significantly affect the frequency of interaction by any mode. Respondents could state whether they owned a half-price ticket or a full exemption for all Swiss transport, a regional pass or a pass for a specific route. These categories were tested separately as well as aggregated in a dummy corresponding to owning a pass versus not owning it. No effect at the 0.05 significance level was found. Similar conclusions were reached, for example, by van den Berg et al. (2015). While acknowledging that some of these results may be due to intrinsic characteristics or limitations of the specific dataset/context, with a high share of respondents owning a public transport pass, we believe that this and other results may suggest that dyad-level variables can be more important determinants of communication patterns than ego socio-demographics and characteristics related to the transport system.

Effects of *ego-alter* (dyad) characteristics

The coefficients estimated for the variables expressing dyad characteristics are substantially more significant than those described in the previous section. A detailed interpretation of these coefficients follows.

Distance

This continuous variable represents the distance (measured as a straight line, in kilometres) between the *ego*'s and each *alter*'s home location. It enters the model in 2 different levels, i.e. positive distance (in logs, given the strongly skewed distribution, evident from mean and median statistics reported in Table 2) and zero distance, i.e. dyads living together. 74% of the *ego-alter* pairs present positive distance between their homes, while 3% of them live together.

In line with previous findings (Carrasco and Miller 2009, Frei and Ohnmacht, 2014, Kowald 2013) and with basic intuition, the effect of distance on interactions is very significant, and in particular we find that higher distances are related to lower face-to-face social interactions. In Figure 2, we simulate the impact of increasing distance between *ego*'s and *alters*' home locations on utility for distances between zero and 500 km. This is computed by adding the mode-specific baseline constants to the values of utility computed considering only the effect of distance.

We observe that the impact of distance on face-to-face is larger than on the other modes. In particular, the second strongest effect on utility is for SMS contact, then for phone and e-mail, although the order of the two latter modes is reversed for distances higher than approximately 90 km. The utility accrued by face-to-face communication is substantially lower for people who live far away than for people living close by. Utility decreases with distance also in the case of contact via phone and SMS, while in the case of e-mail we observe the opposite effect: the utility people get from this type of interaction increases with distance. This pattern in the signs of coefficients is not only observed in the case of distance and it seems to suggest that e-mail is a mode of communication that is used for different purposes and with different people with respect to the other three modes. This finding is supported by previous evidence that tackled the same research question (Frei and Ohnmacht 2014).

As mentioned above, the 'zero distance' category is treated separately, as we use a specific dummy variable for people who live together. In this case, we observe significant coefficients only for face-to-face and phone interactions. Although the former is positive (as expected), the phone coefficient is negative. This could either reflect the fact the people who live together, as they see each other very often, tend not to talk often on the phone more than they do with other people, or be the result of a recalling effect: sometimes when there is a strongly prevalent mode of interaction for a specific person, people may overestimate its frequency and underestimate the frequency of other modes when reporting these figures.

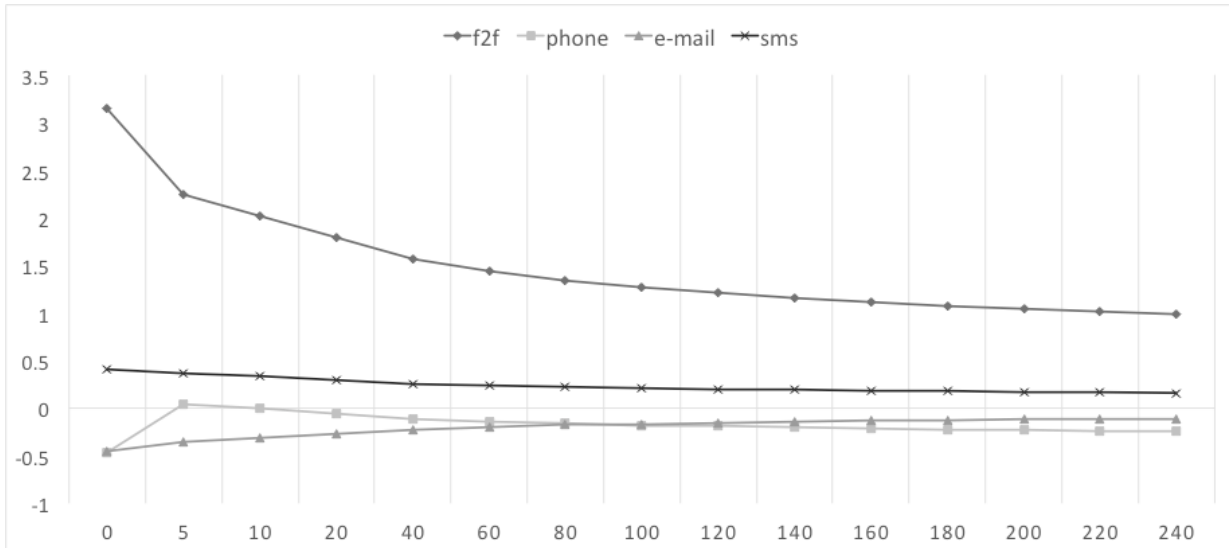


Figure 2 – effect of distance on utility

Relationship duration

This variable indicates for how many years the *ego* and each *alter* have known each other. A log transformation is applied to the values. The coefficients for all the modes are significant and negative except for the phone one, which is positive. This implies that people who have known each other for a long time are more likely to interact via phone than people who have met more recently. Conversely, communication by e-mail, face-to-face and SMS (the coefficients for the last two modes are nearly identical) provides less utility for longer-term relationships than for recently formed ones. It is likely that people who have known each other for long may have relocated to different parts of the city/country, which makes interaction by phone a preferable mode, as it is not as impersonal as other modes but not much affected by distance. Another explanation could be that both people are rather old and will therefore prefer to use the phone. In general, the negative coefficients should not be surprising, as generally long term relationships seem to display lower and lower communication frequencies as time goes by (Kowald 2013, Frei and Ohnmacht, 2014).

Overall, face-to-face is the preferred mode of communication. This can be clearly seen in Figure 3, where we represent the effect of relationship duration on utility given the estimated parameters, analogously to the relationship with distance in Figure 2.

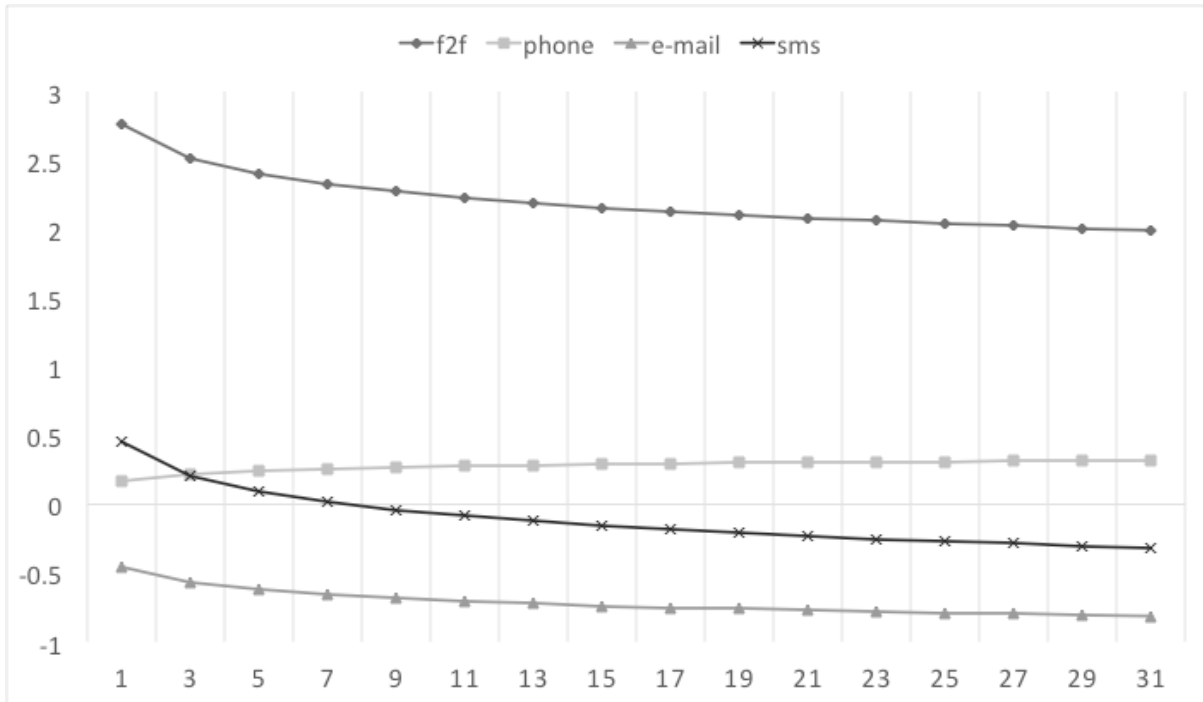


Figure 3 – effect of relationship duration on utility

Age difference

This variable indicates the absolute value of the age difference (in years) between the *ego* and each *alter*. All the coefficients are significant.

From the graph in Figure 4, we can observe that the larger the age difference, the more likely it is that two people will make use of the phone and see each other face-to-face and the less likely it is that they exchange e-mails and SMS. Clearly, when the age difference is large one of the two people is likely to be rather old and not to make large use of new technologies such as computers and mobile phones. As we did for the other continuous exogenous variables, the described dynamics can be graphically visualised by simulating different levels of the variable. In this case the magnitude of the age difference coefficients is rather small for all the modes, so the main effect observed is the one highlighting the comparative preference for the different modes, determined by the alternative specific constants.

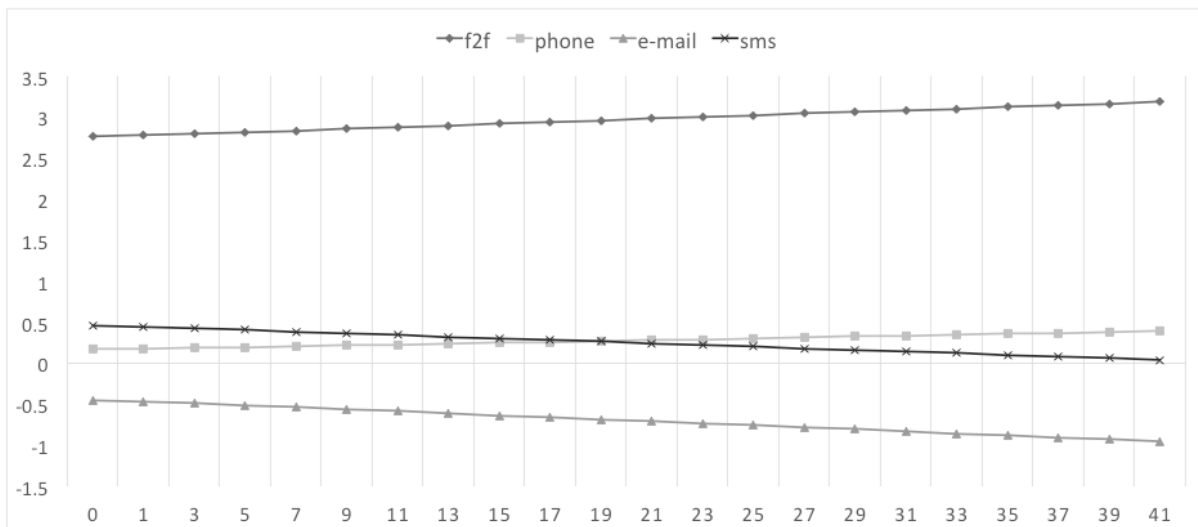


Figure 4 – effect of age difference on utility

Core social contacts

These two dummy variables report the response of the *ego* to the questions “Would you ask the person for help in urgent situations (e.g. when in need of money)?” and “Would you discuss important personal problems with the person (e.g. personal relationships, illness)?” This can be considered a question to detect the people who are very “close” to the *ego*, as she considers them someone to rely on. Respondents could answer Yes (coded as 1) or No (coded as 0). As expected, all the mode-specific coefficients are positive and significant, possibly indicating that people are more likely to interact by any mode with ‘core’ contacts than with people they are not so emotionally close to. The magnitude of the coefficients is generally quite small and mode-specific coefficients are similar for the two variables.

We also included an interaction term between these two variables, to consider the very strong contacts, i.e. the people that the *ego* would both ask for help and discuss problems with. In this case, only the face-to-face coefficient is significant and has positive sign, indicating a more likely interaction with this group of people with respect to others only in person. This finding is in line with the results obtained by Carrasco and Miller (2009).

Sex homophily

We include two different dummy variables related to sex homophily, indicating if both *ego* and *alter* are male and if they are both female. Different sex is used as a base category, as in previous versions of the model it proved not to be significantly different from the case where the value for this variable was missing. We find that if both *ego* and *alter* are male, they are more likely to communicate by any mode except SMS than in communication with the opposite sex. If both are female, they use more phone, e-mail and SMS than when they communicate with the opposite sex, while the face-to-face coefficient is not significant. These results are difficult to compare with most of the other studies which used multilevel models, as they would observe the impact of the *ego* and *alter* socio-economic

characteristics in different levels of the model, i.e. for example Kowald et al. (2013) considers *ego* sex in Level 3 and *alter* sex in Level 2.

Type of relationship

A number of dummy variables are employed to specify whether each *alter* is the *ego*'s spouse, relative of first degree, another relative, someone married into the family, acquaintance or friend. The latter is used as a base category.

We observe a strong significant effect of almost all these variables on communication patterns. The "spouse" coefficients are all positive, implying that *egos* are more likely to communicate by all means with their spouses than with their friends. The face-to-face and phone coefficients are particularly large in magnitude.

Positive signs of all coefficients are also observed in the case of 1st degree relatives, i.e. someone's parents, siblings or children. For more distant relatives and people married into the family we observe lower likelihood of making use of e-mail and SMS than with friends and but more likelihood of using phone. In the case of people married into the family, the face-to-face coefficient is also positive. It is in fact intuitive that contact with family members who are not immediate family will be mostly maintained through occasional phone calls and face-to-face meetings at family gatherings. Our results also reflect previous findings in the sense that SMS seems to be used mainly with very close contacts (like spouses) or family members than with friends (Tillema et al., 2010). The same holds for face-to-face, suggesting the presence of potential complementarities between the two modes. We also observe that although e-mails are likely to be used with very strong contacts like spouses, they are more likely to be used with friends than with not very close relatives and acquaintances.

Education homophily

As mentioned above and highlighted by previous studies, the level of education does not seem to be a determinant of communication frequency. When looking at whether the *ego* and *alter* have the same level of education, we observe that those with the same level tend to interact by e-mail and SMS more than those with a different level. The opposite holds for face-to-face, suggesting that it is more likely for two people with a different level of education to meet in person than for people with the same level. Communicating with someone with a different level of education could be relatively more difficult, and the richness of expression possible with face-to-face can be a way to overcome such difficulty.

Citizenship homophily

Most of the respondents have been recruited in the Zurich area, but not all their social contacts are Swiss citizens. We therefore added a variable to assess the influence of being citizens of the same country, which also implies being native speakers of the same language, on communication. The nationalities reported by participants were Swiss, German, Austrian, Italian, French and Other. Evidence of a preference for co-nationals is not completely

unexpected, and is also supported by recent work on residential location choices in the Swiss city of Lugano (Ibraimovic & Hess, 2016) We observed that this variable is only significant (and positive) in the case of face-to-face and SMS, giving us a hint on possible complementarities between these two modes.

4.2. Missing values analysis

The name generator technique applied to collect the data used for the present study presents a number of issues when it comes to the reliability of the information reported by respondents. One problem which has been addressed by previous research is the accuracy of the reported network composition, as people are more likely to remember those social contacts who are emotionally closer to them (Bell et al., 2007; Marin 2004).

Another often observed problem is the difficulty encountered by respondents when it comes to recalling information about the *alters* that they name, for example because of fatigue or satisficing behaviour (Pustejovsky and Spillane, 2009) or simply lack of knowledge of the requested information.

We hypothesised that the presence of missing values might not have been random in the dataset, and that by modelling these values as a separate category of exogenous variables we could have tried to interpret results and understand the reasons behind non-reporting. In addition, elimination of all the *egos* who reported missing information for at least one of their *alters* would have resulted in massive loss of observations.

It is sometimes relatively easy to provide an interpretation of the coefficients estimated for the dummy variables indicating a missing value, while in other occasions this is not the case. Most of the missing values were due to lack of information about *alters*, with the only exception of *ego* years of education. The corresponding coefficients are reported in the first line of the “Missing values coefficients” section of Table 4 (although they are not significant), followed by a number of dyad measures.

In the case in which the *ego* did not report his or an *alter's* home location, it was not possible to compute the distance and the variable was treated as missing. In this case, we find significant and negative coefficients for communication face-to-face, by phone and via SMS, meaning that people who do not provide addresses are less likely to communicate by these modes than those who do. As most of the missing values were at the *alter*-level, this could be interpreted by hypothesising that if an *ego* does not know where the *alter* lives he either does not know this person very well, or the person lives too far for the *ego* to provide an accurate address. If this is true, it would make sense to imagine that there will not be intensive communication between them.

A similar interpretation seems to be applicable in several other cases, for example in the case of education homophily, where the *ego* is asked to report both his and the *alters'* level of education. It is reasonable that the *alter's* education level is not known by the *ego* for

loose social network members. Also in the case of missing values for age difference (generally implying that the *alters'* age is not reported) it makes sense to observe that those are people with whom there is no intensive face-to-face or phone interaction. The positive coefficient on e-mail might indicate that there is more likely to be “distant” or maybe work-related interaction by e-mail with these people with respect to the ones whose personal information such as age are known to the *ego*.

In the case of relationship duration, we observe that the coefficients in the missing values case present the same signs as the case when values are stated, although the absolute magnitudes are slightly higher in the first case. A possible reason for non-reporting this piece of information is that the *ego* could have known the *alter* for a long time and could not be able or willing to recall the exact number of years, as this is the way the question was posed. If this is the case, a similar effect on utility in the two cases would not be very surprising.

In some cases, like when the type of relationship with the *alter* is not specified by the *ego*, there is no intuitive interpretation of the missing values coefficients, as all the possible categories were included in the multiple-choice question. In our case, none of the coefficients are significant. Also, the missing values in the simple Yes/No questions asking *egos* whether they ask a given *alter* for help or discuss problems with them are not easy to interpret. One possible interpretation is that participants decided to skip this question in cases it required them to much thinking/recalling, i.e. in cases when the *alter* was neither someone very emotionally close to them, nor an acquaintance. This would explain the positive face-to-face coefficient for “Discuss problems” and the positive phone one for “Ask for help”, meaning that these are people who are in touch with the *ego* but not too closely. The opposite signs of the e-mail coefficients and the negative one for the SMS ones are more open to different interpretations.

The separate modelling of the missing values is an important approach in our application. Not only we can learn more about the phenomenon that we are investigating, i.e. the communication patterns, but we can also infer recommendations about survey design, as these coefficients can suggest, for example, that one should not aim at collecting too large and loose networks because the quality and availability of information about the *alters* decreases the more “affectively distant” they are from the *ego*. This approach is also the most appropriate in terms of modelling: we have indeed tested whether separate coefficients for the missing values were to be necessarily included or if the implied values were not significantly different from the mean (in the case of continuous variables). It was not the case, and therefore we had to treat them separately, also given that many of them were significant.

5. Model forecast

An interesting question related to the topic studied in the present paper is to what extent the pattern of communication between an ego and her social contacts changes if there is a change in the characteristics of one of the alters, for example if a friend moves further away from the ego. In order to investigate this issue, we applied the forecasting procedure for MDCEV models proposed by Pinjari & Bhat (2010).

In particular, we selected a subsample of our dataset that only includes egos who reported a friend who lives less than 5 km away from them (excluding friends who live with them). If more than one contact with these characteristics existed, we only considered one of them, in particular, the first one reported in the name generator. This resulted in a sample of 398 people. Following Pinjari & Bhat (2010), we computed the frequencies of interaction with all the alters in the base scenario and in the forecasting scenario, when the selected friend's distance to the ego is increased by 10%.

In order to summarise the effect of the change, the forecasting results were used to compute elasticities of the frequency of interaction and of distance travelled across the sample of respondents. These are displayed in Table 5.

<i>Elasticities of the frequency of interaction by each mode</i>	
<i>face-to-face</i>	-0.004
<i>phone</i>	0.002
<i>e-mail</i>	0.008
<i>SMS</i>	0.003
<i>Elasticities of the frequency of interaction with relocated alter by each mode</i>	
<i>face-to-face</i>	-0.162
<i>phone</i>	-0.037
<i>e-mail</i>	0.052
<i>SMS</i>	-0.028
<i>Overall elasticity of the frequency of interaction</i>	-8E-06
<i>Elasticity of the frequency of interaction with the relocated alter</i>	-0.075
<i>Elasticity of consumption of the outside good</i>	0.006
<i>Distance elasticity</i>	0.007
<i>Distance elasticity for relocated alter</i>	-0.011

Table 5

These results provide some important insights. First of all, we can observe that the overall frequency of interaction with social contacts is inelastic with respect this change. The elasticities of the frequency of interaction by each mode also underline that a change in distance will cause a reduction of overall face-to-face contact only, as obviously increased distance will mainly impact this type of interaction.

Overall distance travelled is computed for each ego by multiplying the ego-alter distance for the number of yearly face-to-face contacts and dividing by 2. We are aware that this is an approximation, but as previously stated the data do not contain any information about meeting locations. The computed distance elasticity is small and negative for the relocated alter, meaning that the ego will travel less to see this alter. However, the overall elasticity is

positive (though also small), meaning that there is a positive overall impact on the overall distance travelled, so that the ego compensates the drop in travel to the affected alter with more travel to other alters.

As expected, we observe a greater value for the elasticities of the frequency of interaction with the relocated social contact. Not only face-to-face interactions are sensitive to the increase in distance, but also the variation in phone and SMS, although smaller, is found to be negative. This finding potentially highlights the role of the latter two modes as complementary to face-to-face and as being used mainly for coordination purposes with contacts who live close by. E-mail frequency, in line with the overall findings of the model, seems to be likely to increase following an increase in distance. These results hint at the potential presence of substitution effects between face-to-face and ICT, which Sharmeen et al. (2013) already suggested to be strongly related to distance. Finally, we observe that the overall elasticity of interactions with the relocated alter is negative, meaning that overall, the ego will interact less with this person. Differently from our findings, Sharmeen et al. (2014) suggested a positive coefficient for interactions with a relocated alter, though acknowledging the counterintuitive result. Moreover, the authors tested the effect of a neighbour relocation, while our case concerns friends: these findings could highlight the importance of considering dyad-level characteristics such as relationship type to capture an accurate behavioural picture.

Although these results provide interesting insights about the sensitivity of the frequency of interaction to a change in distance between two people, it is important to point out that our forecasts are based on a model estimated on cross-sectional data. Over time, an ego has put together a network of alters that he/she interacts with and the specific pattern of interactions has evolved over that time. This in turn means that the impact distance has on frequency of interaction in the data is reflecting interaction patterns in some continuously evolving and partially stable situation. If an alter moves further away from the ego, then this may reduce interaction, but the effect may be more or less than the difference in the level of interaction at the “partially stable state” with two alters who are otherwise identical but live at different distances from the ego. Only the availability of longitudinal data with some location changes by alters or egos would allow us to truly understand the impact that changes in distance will have on interaction patterns. For this reason, the present exercise is likely to overstate the impact, at least in the short term.

As reported in section 3.2, we estimated versions of the model where the budget was increased by the same amount for the entire sample, and when the prices differed across modes. We applied the forecasting routine also to these models to check whether these different assumptions about the budget and prices would affect elasticities. The results, presented in our online appendix, show that there are no substantial differences in the elasticities obtained from the models where different assumptions on the budget and the prices are applied.

6. CONCLUSIONS AND FUTURE RESEARCH

Our study investigated the determinants of communication frequency by four modes (face-to-face, phone, e-mail, and SMS) between people and their social network members.

Its findings contribute not only to a better understanding of social networks, but also provide interesting insights for the analysis of travel behaviour for social and leisure purposes.

In terms of understanding communication patterns, we gave a detailed picture of mode-specific determinants of communication, advancing the study of this topic by using a model which simultaneously examines the contribution to utility of communication of both individual and *ego-alter* characteristics. On top of showing the detailed effect of each of these variables, we provide a picture of satiation effects from different communication modes, showing that despite face-to-face meetings remaining the most preferred type of communication, a lower number of interactions are demanded for each network member with respect to the other modes.

Our work also provides interesting insights into the modelling of travel behaviour, as understanding the pattern of interaction between leisure network members helps to understand travel for social and leisure purposes. The confirmation of the presence of a strong underlying preference for face-to-face contact (especially in the maintenance of core contacts) is an important conclusion given the ongoing debate on potential substitution effects between ICT based modes of communication and most traditional ones.

Additionally, we have shown that while some of the results linking socio-demographics to social interactions patterns are in line with results from previous work, other findings highlight differences that are particularly interesting for travel behaviour analysis. In particular, according to our results, the availability of specific travel modes or public transport passes does not seem to significantly affect the frequency of communication. Previous studies do not present clear-cut evidence on the significance of these factors for the patterns of social interactions, so we acknowledge that our findings could be partially related to the specific context where the data was collected as well as to the lack of detailed information about the transport network. These results could also possibly suggest that some of the existing travel behaviour work mainly focussing on travel-related variables and ego-level characteristics as determinants of decisions about social activity travel might not have fully considered other important aspects that can be investigated while making use of social network data. Moreover, differently from similar studies which made use of social network data, the simultaneous modelling technique adopted in the present paper allows us to observe that dyad level variables have a much more significant effect on communication frequency than *ego*-level ones, a result that supports the need to make use of measures related to the similarities and differences between *egos* and *alters* to understand interaction patterns. A brief illustrative forecasting example also shows how a

model of the type used here can be used to gain insights into the likely changes in travel patterns resulting from changes in the composition and characteristics of a social network.

The findings and the modelling framework also has implications for the design of activity-based models. As previous research and this work have shown, face-to-face meetings depend on communication patterns at the level of an individual's social network. Thus, these communication models can be used to determine the probability of an individual generating social activities in their daily activity patterns. Additionally, the communication model gives an indication of what types of in and out-of-household contacts are likely meet and the frequency of this contact. Thus, the model also helps to enhance ABMs that include the coordination of joint inter- and intra-household activities. These enhancements will have important considerations as segments of society move toward less car ownership and vehicle sharing.

The present work constitutes a first step in the use of MDCEV models in the investigation of communication frequencies, and several improvements and more flexible structures can be suggested to better represent this specific behavioural process.

A first issue that we raised is the use of this model when the budget specification is not clear-cut. Both investigating the use of simplified approaches like in this paper and the attempt to derive prices and budgets which are not observed can constitute an interesting next step in this work.

In this paper, we estimated one γ parameter for each mode of communication to avoid explosion in the number of parameters. Nevertheless, heterogeneity in satiation could be accommodated in ways other than estimating one γ for each product. A possible option would be to parameterise the four mode-specific γ s as a function of observed ego- and dyad-level characteristics to investigate whether these can affect satiation. We aim to perform a detailed investigation of this research question in future work on this topic.

Moreover, as mentioned while presenting the model results, we have observed that the signs and magnitudes of coefficients suggest the possible presence of complementarities between different modes while in other cases the substitution effects were more evident. The limiting case of perfect substitution between different modes can also not be excluded. The presence of these complex patterns is supported by existing literature, e.g. Sharmeen et al. (2013). The current version of the model, by only allowing the consideration of imperfect substitute goods, does not allow us to test these hypotheses. An extension of the present work to test for more flexible complementarity and substitution patterns is an important area for future work. This could involve developing a nested version of the current model, or relying on model extensions such as Bhat et al. (2015). Finally, as highlighted in the forecasting example, an important next step would be the use of longitudinal data in a study of this type.

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Table 4 – Model results

	<i>face-to-face</i>		<i>phone</i>		<i>e-mail</i>		<i>SMS</i>	
	est	t-stat	est	t-stat	est	t-stat	est	t-stat
<i>y parameters</i>	0.5567	23.92	3.0200	51.67	5.6150	47.34	7.7260	43.35
<i>Baseline constants (δ)</i>	4.3710	14.92	1.4810	5.06	-0.1050	0.34	0.4197	1.37
<i>Ego characteristics</i>								
<i>Age</i>								
Age = 18	0.0712	0.12	-0.0372	0.06	-2.1840	3.38	0.7791	1.26
Age 19-30	-0.1515	0.61	-0.4043	1.62	-0.5198	2.04	0.7626	2.99
Age 31-45	-0.0415	0.25	-0.0942	0.57	0.0703	0.42	0.5786	3.37
Age 46-60	-0.0999	0.63	-0.1928	1.21	-0.0300	0.18	0.4215	2.52
<i>Education duration (years)</i>	-0.0141	1.25	-0.0101	0.88	0.0311	2.69	-0.0211	1.80
<i>Civil status</i>								
Married	-0.0744	0.51	-0.2604	1.77	-0.4053	2.72	-0.5950	3.99
Widowed	-0.0827	0.33	-0.3542	1.39	-0.9495	3.54	-0.4597	1.74
Divorced	-0.1570	0.78	-0.2907	1.43	-0.5044	2.44	-0.4056	1.96
Living separately	-0.2679	0.67	-0.0515	0.13	-0.6754	1.66	-0.3348	0.82
<i>Employment status</i>								
Student	0.3020	0.98	-0.1467	0.47	0.4092	1.31	0.1495	0.48
Homemaker	-0.0506	0.36	-0.0711	0.51	-0.2290	1.59	-0.1590	1.10
Retired	-0.1903	1.05	-0.1912	1.05	-0.4997	2.68	-0.4710	2.43
Looking for work	-0.2901	0.87	-0.0433	0.13	0.1712	0.50	-0.0467	0.14
<i>Number of contacts</i>	-0.0083	2.05	-0.0130	3.20	-0.0016	0.39	-0.0001	0.02
<i>Ego-alter characteristics</i>								
<i>Distance</i>	-0.3250	43.40	-0.075	10.28	0.063	7.47	-0.0538	0.01
<i>Distance=0</i>	0.3900	5.22	-0.6403	8.51	-0.0005	0.00	-0.0462	0.51
<i>Relationship duration</i>	-0.2360	17.94	0.0436	3.01	-0.1078	6.18	-0.2271	12.27
<i>Sex homophily</i>								
Both male	0.0667	2.33	0.0672	2.19	0.3242	8.92	-0.2741	6.28

<i>Both female</i>	0.0093	0.04	0.2510	9.79	0.0858	2.64	0.4698	13.82
<i>Age difference</i>	0.010	10.15	0.0054	4.94	-0.0122	8.06	-0.0101	6.52
<i>Help & Problems</i>								
Ask for help	0.2733	5.01	0.4673	8.11	0.3353	4.61	0.3069	3.73
Discuss problems	0.2373	9.06	0.4483	16.03	0.2305	6.64	0.4947	13.07
Ask for help x Discuss problems	0.1545	2.59	-0.0668	1.06	-0.1434	1.81	-0.1391	1.58
<i>Type of relationship</i>								
Spouse	2.1530	26.86	1.1950	15.22	0.2216	2.24	0.9860	10.35
Relative 1st degree	0.5001	14.47	0.5084	14.04	0.0112	0.24	0.3530	7.23
Relative	-0.0291	0.68	0.0608	1.36	-0.3955	6.16	-0.0786	1.19
Married into family	0.1171	2.65	0.1381	2.96	-0.5771	8.33	-0.3397	4.68
Acquaintance	-0.2245	8.82	-0.3868	13.85	-0.1176	3.53	-0.5809	14.90
<i>Same level of education</i>	-0.0433	2.00	-0.0242	1.05	0.1246	4.28	0.1092	3.51
<i>Same citizenship</i>	0.1085	3.91	0.0285	0.94	0.0272	0.75	0.1069	2.64
<i>Missing values coefficients</i>								
<i>Ego education duration</i>	0.7742	1.35	-0.4215	0.73	0.8407	1.43	-0.4971	0.82
<i>Distance</i>	-0.9766	27.85	-0.2386	6.70	-0.0416	0.98	-0.1308	2.89
<i>Relationship duration</i>	-0.5914	6.22	0.3452	3.61	-0.7104	5.55	-0.9118	7.25
<i>Age difference</i>	-0.4591	7.05	-0.4893	6.94	0.4654	5.28	0.0283	0.29
<i>Ask for help</i>	0.1899	1.58	0.3669	2.82	-0.4536	2.48	-0.4743	2.16
<i>Discuss problems</i>	0.3971	2.92	-0.1233	0.81	0.3689	1.98	-0.6967	2.59
<i>Type of relationship</i>	-0.0217	0.19	-0.1860	1.44	-0.1018	0.63	-0.0272	0.17
<i>Same level of education</i>	-0.1045	2.70	-0.1653	4.13	0.0453	0.97	-0.0830	1.65
<i>Log-likelihood: -162,036.9</i>								

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